

Geometry
Triangle Angles

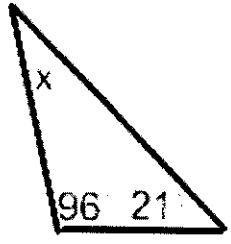
Name: Keyz
Date: _____

TRIANGLE SUM

The sum of the measures of the interior angles of a triangle is 180°.

Find the value of x in each figure.

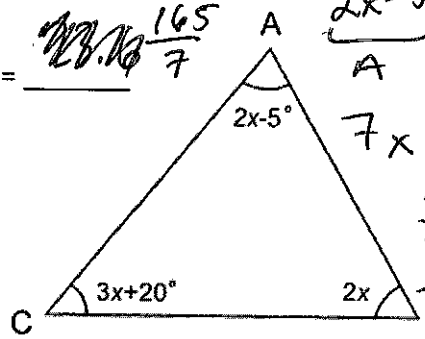
1. $x = \underline{63^\circ}$



$$\begin{array}{r} x + 96 + 21 = 180 \\ x + 117 = 180 \\ -117 \quad -117 \\ \hline x = 63^\circ \end{array}$$

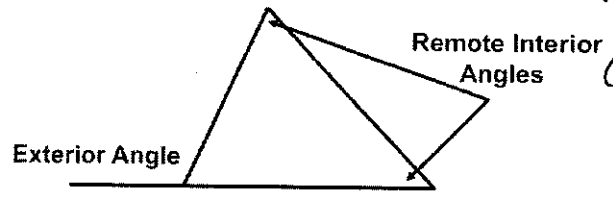
2. $x = \underline{\frac{165}{7}}$

$$\begin{array}{r} 2x - 5 + 2x + 3x + 20 = 180 \\ \hline 7x + 15 = 180 \\ -15 \quad -15 \\ \hline 7x = 165 \\ \hline x = \frac{165}{7} \end{array}$$



EXTERIOR ANGLE THEOREM

The measure of an exterior angle of a triangle is equal to the **sum** of the measures of the two remote interior angles.

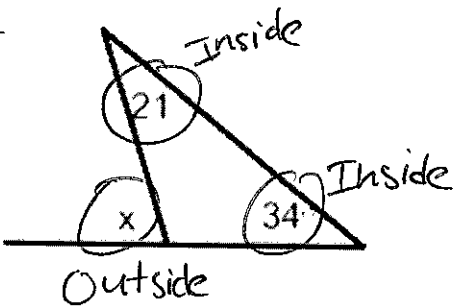


(Doesn't simplify)

"INSIDE + INSIDE = OUTSIDE"

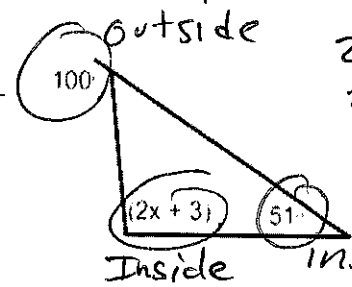
Find the value of x in each figure.

3. $x = \underline{55^\circ}$



$$\begin{array}{r} 21 + 34 = x \\ 55 = x \end{array}$$

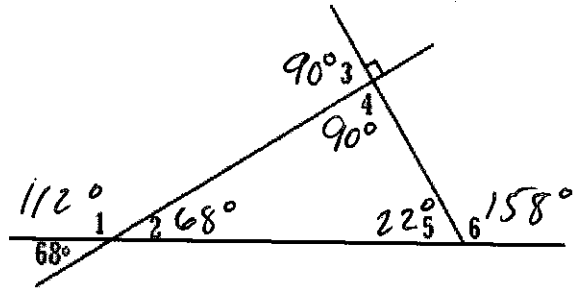
4. $x = \underline{23}$



$$\begin{array}{r} 2x + 3 + 51 = 100 \\ 2x + 54 = 100 \\ -54 \quad -54 \\ \hline 2x = 46 \\ \hline x = 23 \end{array}$$

Find the value of each numbered angle.

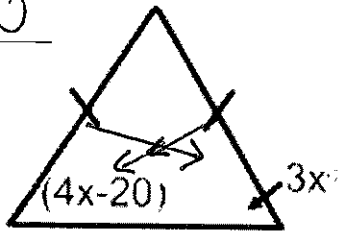
5. $m\angle 1 = \underline{112^\circ}$
6. $m\angle 2 = \underline{68^\circ}$
7. $m\angle 3 = \underline{90^\circ}$
8. $m\angle 4 = \underline{90^\circ}$
9. $m\angle 5 = \underline{22^\circ}$
10. $m\angle 6 = \underline{158^\circ}$



Isosceles Triangles & Base Angles

If two **sides** of a triangle are congruent, then the **angles opposite** those sides are **congruent**.

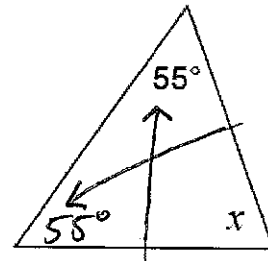
5. $x = 20$



$$\begin{array}{r} 3x = 4x - 20 \\ -4x \quad -4x \\ \hline -x = -20 \end{array}$$

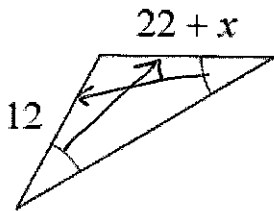
6. $x = 70^\circ$

$$\begin{array}{r} 55 + 55 + x = 180 \\ 110 + x = 180 \\ -110 \quad -110 \\ \hline x = 70 \end{array}$$



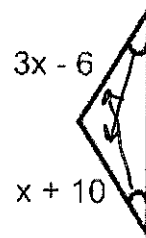
If two **angles** of a triangle are congruent, then the **sides opposite** those angles are **congruent**

7. $x = -10$



$$\begin{array}{r} 12 = 22 + x \\ -22 \quad -22 \\ \hline -10 = x \end{array}$$

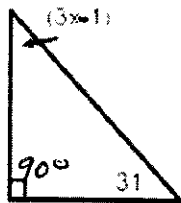
8. $x =$ _____



$$\begin{array}{r} x + 10 = 3x - 6 \\ -10 \quad -10 \\ \hline x = 3x - 16 \\ -3x \quad -3x \\ \hline -2x = -16 \\ \frac{-2x}{-2} = \frac{-16}{-2} \\ \boxed{x = 8} \end{array}$$

PRACTICE!!!

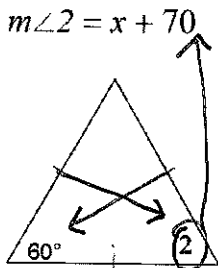
1. $x = 20$



$$3x - 1 + 31 + 90 = 180$$

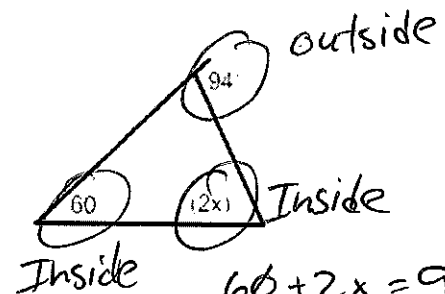
$$\begin{array}{r} 3x + 120 = 180 \\ -120 \quad -120 \\ \hline 3x = 60 \end{array}$$

3. $x = -10$



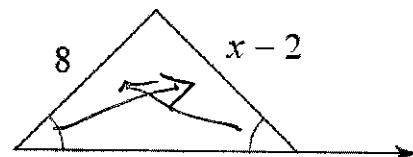
$$\begin{array}{r} 60 = x + 70 \\ -70 \quad -70 \\ \hline -10 = x \end{array}$$

2. $x = 17$



$$\begin{array}{r} 60 + 2x = 94 \\ -60 \quad -60 \\ \hline 2x = 34 \\ \frac{2x}{2} = \frac{34}{2} \end{array}$$

4. $x = 10$

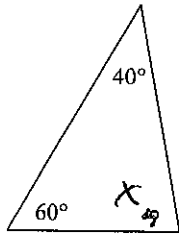


$$\begin{array}{r} x - 2 = 8 \\ +2 \quad +2 \\ \hline x = 10 \end{array}$$

Triangle Sums

Find the measure of each angle indicated.

1)



$$\begin{aligned} 60 + 40 + x &= 180 \\ 100 + x &= 180 \\ -100 &\quad -100 \\ \hline x &= 80 \end{aligned}$$

$x = 80^\circ$

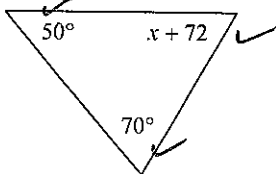
2)



$$\begin{aligned} x + 90 + 70 &= 180 \\ x + 160 &= 180 \\ -160 &\quad -160 \\ \hline x &= 20^\circ \end{aligned}$$

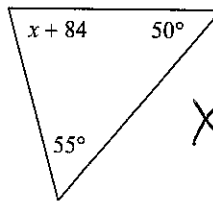
Solve for x.

3)



$$\begin{aligned} 50 + 70 + x + 72 &= 180 \\ 192 + x &= 180 \\ \hline x &= -12 \end{aligned}$$

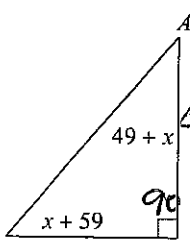
4)



$$\begin{aligned} x + 84 + 50 + 55 &= 180 \\ x + 189 &= 180 \\ -189 &\quad -189 \\ \hline x &= -9 \end{aligned}$$

Find the measure of angle A.

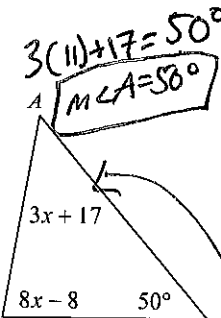
5)



$49 + (-9) = 40^\circ = m\angle A$

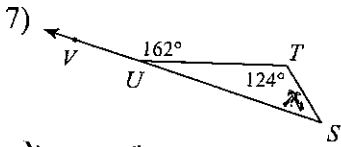
$$\begin{aligned} x + 59 + 90 + 49 + x &= 180 \\ 2x + 198 &= 180 \\ -198 &\quad -198 \\ \hline 2x &= -18 \\ \frac{2x}{2} &= \frac{-18}{2} \\ x &= -9 \end{aligned}$$

6)



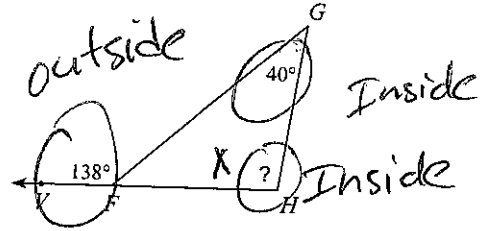
$$\begin{aligned} 3(11) + 17 &= 50^\circ \\ m\angle A &= 50^\circ \\ 3x + 17 + 50 + 8x - 8 &= 180 \\ 11x + 59 &= 180 \\ -59 &\quad -59 \\ \hline 11x &= 121 \\ \frac{11x}{11} &= \frac{121}{11} \\ x &= 11 \end{aligned}$$

Find the measure of each angle indicated. **INSIDE+INSIDE=OUTSIDE**



$$\begin{array}{r} x + 124 = 162 \\ -124 \quad -124 \\ \hline x = 38 \end{array}$$

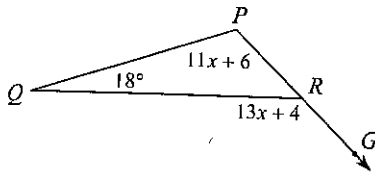
8)



$$\begin{array}{r} 40 + x = 138 \\ -40 \quad -40 \\ \hline x = 98 \end{array}$$

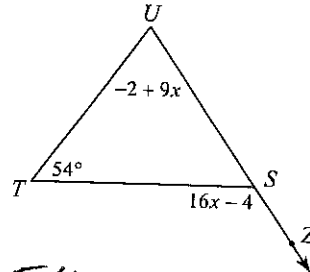
Solve for x.

9)



$$\begin{array}{r} 18 + 11x + 6 = 13x + 4 \\ 11x + 24 = 13x + 4 \\ -11x \quad -4 \quad -11x \quad -4 \\ \hline 20 = 2x \\ \frac{20}{2} = \frac{2x}{2} \quad x = 10 \end{array}$$

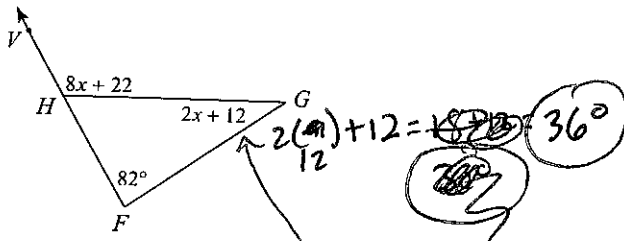
10)



$$\begin{array}{r} 54 + -2 + 9x = 16x - 4 \\ 52 + 9x = 16x - 4 \\ +4 \quad -9x \quad -9x + 4 \\ \hline 56 = 7x \quad x = 8 \end{array}$$

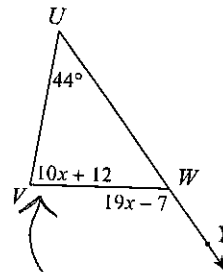
Find the measure of the angle indicated.

11) Find $m\angle G$.



$$\begin{array}{r} 82 + 2x + 12 = 8x + 22 \\ 2x + 94 = 8x + 22 \\ -2x \quad -22 \quad -2x \quad -12 \\ \hline 72 = 6x \\ \frac{72}{6} = \frac{6x}{6} \quad x = 12 \end{array}$$

12) Find $m\angle V$.



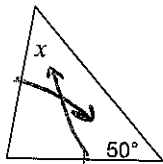
$$\begin{array}{r} 44 + 10x + 12 = 19x - 7 \\ 10x + 56 = 19x - 7 \\ -10x + 7 \quad -10x + 7 \\ \hline 63 = 9x \\ \frac{63}{9} = \frac{9x}{9} \\ x = 7 \end{array}$$

$10(7) + 12 = 82^\circ$

Base Angle Theorem Classwork

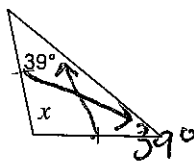
Find the value of x .

1)



$$x = 50^\circ$$

2)

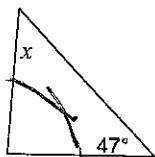


$$39 + 39 + x = 180$$

$$\begin{array}{r} 78 + x = 180 \\ -78 \quad -78 \\ \hline \end{array}$$

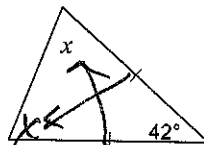
$$x = 102^\circ$$

3)



$$x = 47^\circ$$

4)



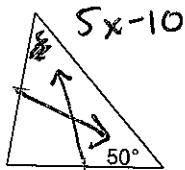
$$x + x + 42 = 180$$

$$\begin{array}{r} 2x + 42 = 180 \\ -42 \quad -42 \\ \hline \end{array}$$

$$\frac{2x = 138}{2 \quad 2}$$

$$x = 69^\circ$$

5) $m\angle 2 = 5x - 10$

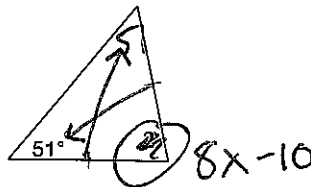


$$\begin{array}{r} 5x - 10 = 50 \\ +10 \quad +10 \\ \hline \end{array}$$

$$\frac{5x = 60}{5 \quad 5}$$

$$x = 12$$

6) $m\angle 2 = 8x - 10$



$$51 + 51 + 8x - 10 = 180$$

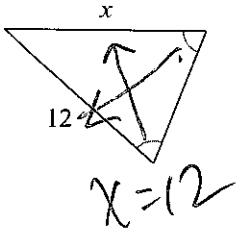
$$102 + 8x - 10 = 180$$

$$\begin{array}{r} 92 + 8x = 180 \\ -92 \quad -92 \\ \hline \end{array}$$

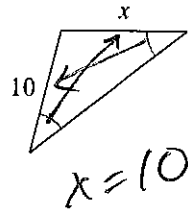
$$\frac{8x = 88}{8 \quad 8}$$

$$x = 11$$

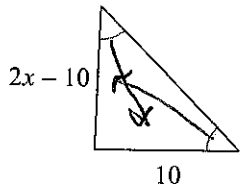
7)



8)

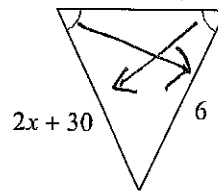


9)



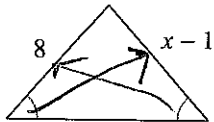
$$\begin{array}{r} 2x - 10 = 10 \\ +10 \quad +10 \\ \hline 2x = 20 \\ \frac{2x}{2} = \frac{20}{2} \\ x = 10 \end{array}$$

10)



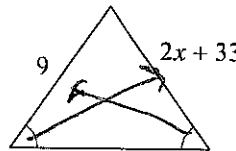
$$\begin{array}{r} 2x + 30 = 6 \\ -30 \quad -30 \\ \hline 2x = -24 \\ \frac{2x}{2} = \frac{-24}{2} \\ x = -12 \end{array}$$

11)



$$\begin{array}{r} 8 = x - 1 \\ +1 \quad +1 \\ \hline x = 9 \end{array}$$

12)



$$\begin{array}{r} 9 = 2x + 33 \\ -33 \quad -33 \\ \hline -24 = 2x \\ \frac{-24}{2} = \frac{2x}{2} \\ x = -12 \end{array}$$